

5-5 Integral Applications

Learning Objectives:

I can use integration to solve real world problems.

I can use integration to calculate displacement and total distance traveled.

Nov 26-11:11 AM

Ex1. Water is entering/exiting a tank. $r(t)$ represents the rate at which water is entering/exiting the tank at time t .

t	r(t)
0	2
1	7
5	10
8	3
10	-2
18	5

a.) Approximate $\int_0^{18} r(t)dt$ using a right rectangle approximation method

b.) Explain the meaning of this integral using proper units.
 change in volume (cubic feet) from time $t=0$ minutes to 18 minutes.

c.) Find the rate of change in the depth of the water with respect to time when $t=5$ min.

Indicate the units of measure. Assume that the tank is a rectangular box that is 5 by 10 by 4.

$\frac{dh}{dt} = ?$
 $\frac{dV}{dt} = 10$

$V = lwh$
 $V = 50h$

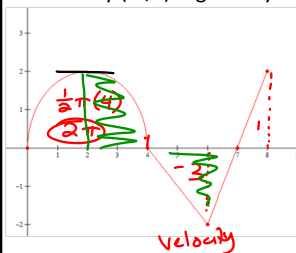
$\frac{dV}{dt} = 50 \frac{dh}{dt}$

$10 = 50 \frac{dh}{dt}$

$\frac{dh}{dt} = \frac{1}{5} \text{ ft/min}$

Nov 26-11:11 AM

Ex2. An object is moving back and forth on the number line. Its velocity (m/s) is given by the graph below.



- a.) Find $\int_0^8 v(t)dt$
 Explain the meaning of this integral using appropriate units.
Change in position (meters) from 0 to 8 seconds
 $2\pi - 2$ meters
- b.) Find the total distance traveled by the object from $t=2$ sec to $t=7$ sec.
 $\pi + 3$ meters
- c.) Find the acceleration of the object at time $t=2$ sec and at time $t=7$ sec.
 0 m/sec^2
 2 m/sec^2

Nov 26-11:11 AM

Homework

pg 312 # 9-12, 31-36

Nov 26-11:11 AM